



# How Neighborhood Exploration influences Novelty and Diversity in Graph Collaborative Filtering

Vito Walter Anelli, Yashar Deldjoo, Tommaso Di Noia, Eugenio Di Sciascio,  
Antonio Ferrara, Daniele Malitesta, Claudio Pomo

*Politecnico di Bari*

*Bari, Italy*

*email: [firstname.lastname@poliba.it](mailto:firstname.lastname@poliba.it)*

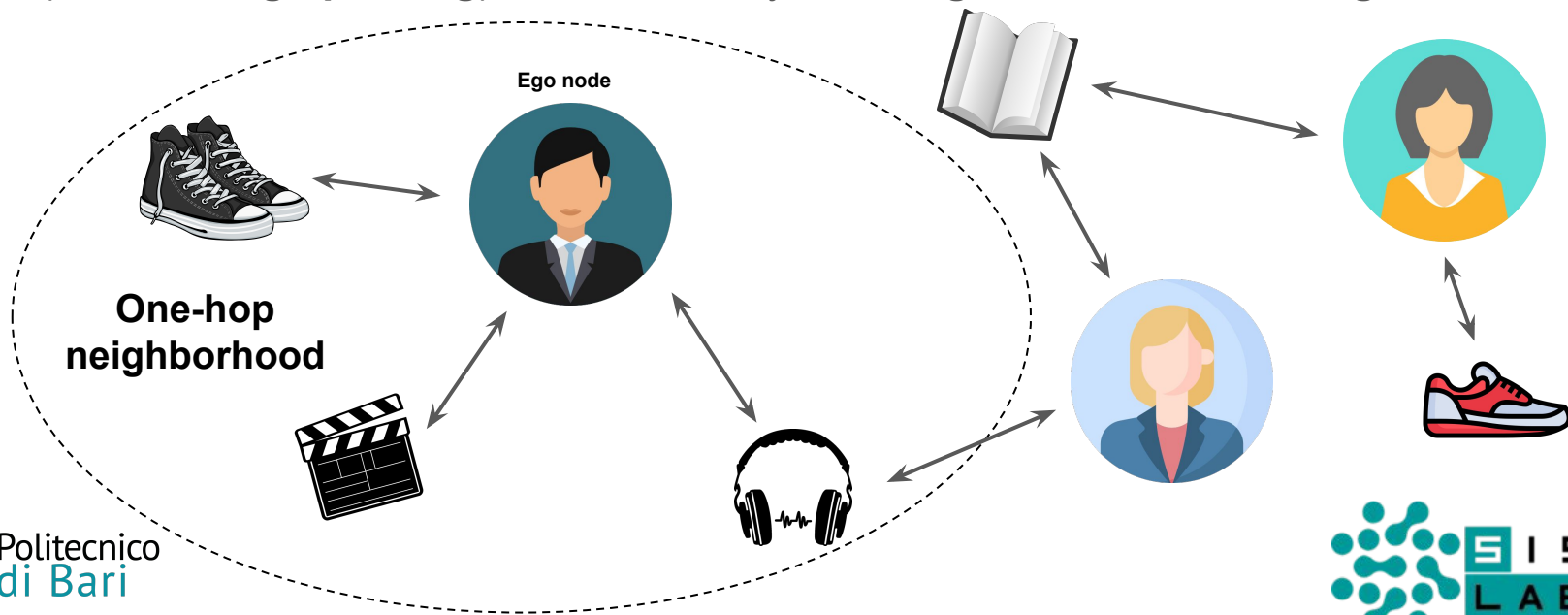


# Introduction and Contributions



# Graph collaborative filtering

In collaborative filtering (CF), graph convolutional networks (GCNs) have gained momentum thanks to their ability to **aggregate neighbor nodes information** into ego nodes at multiple hops (i.e., **message-passing**), thus effectively **distilling the collaborative signal**.

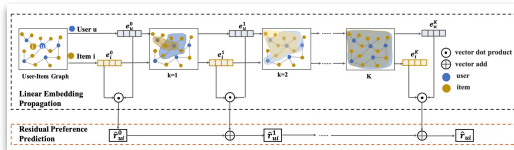
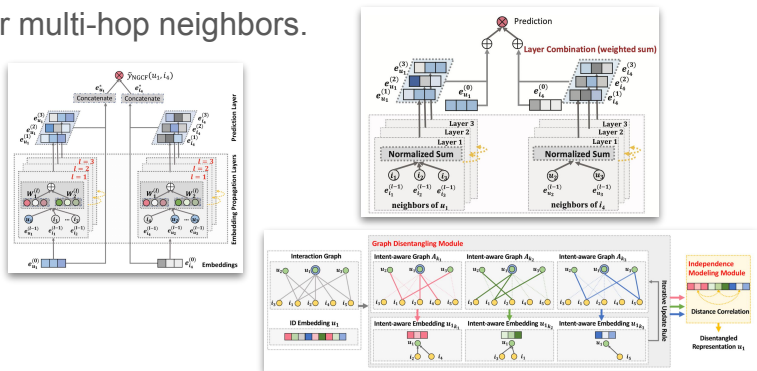




# Neighborhood exploration strategies

## Explicit message-passing

It is always possible to derive a **formulation** where user and **item** node representations are **explicitly updated** through their multi-hop neighbors.



## Implicit message-passing

We **introduce** the concept of **implicit** message-passing, where message aggregation is **replaced** and improved through ad-hoc **mathematical proxies**.

$$s_u = r_u \left( \tilde{R}^T \tilde{R} + \alpha D_I^{-\frac{1}{2}} \tilde{U} \tilde{U}^T D_I^{\frac{1}{2}} \right)$$

$$\mathcal{L}_I = - \sum_{(u,i) \in N^+} \sum_{j \in \mathcal{S}(i)} \omega_{i,j} \log(\sigma(e_u^T e_j))$$



# Multi-objective recommendation and graph CF

Graph CF has shown **remarkable results** on the sole recommendation **accuracy**. However, designing RSs trying to **optimize multiple objectives** at once is the new goal in the recent literature, as a way to embrace both **users' and business' interests**.

So far, in graph CF:

- **limited attention** put on the **accuracy-diversity** trade-off
- **no in-depth analysis** of the **neighborhood exploration** influence

**Our contributions:**

- ❖ assessment of the **accuracy-novelty-diversity** recommendation **trade-off** of **explicit** and **implicit** message-passing models from the state-of-the-art (**six** baselines)
- ❖ simple **mathematical reformulation** of **explicit** message-passing, where **same-** and **different-type** node explorations are highlighted, and **extend** the trade-off study **analysis** on this **new dimension**

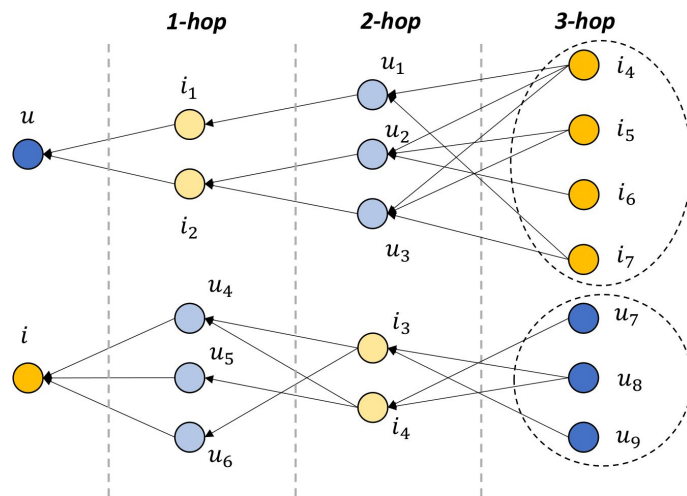


# Explicit message-passing reformulation



# Useful notation

- $e_u^{(0)}$ ,  $e_i^{(0)}$  are the user/item node embeddings
- $\omega(\cdot)$  is the message aggregation function
- $\mathcal{N}(\cdot)$  is the neighborhood of the ego node





# Message-passing reformulation (1/2)

After one hop (Eq.1):

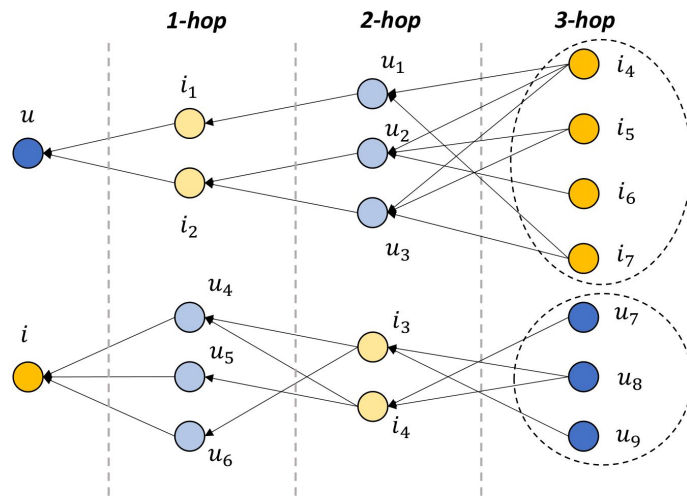
$$\mathbf{e}_u^{(1)} = \omega \left( \left\{ \mathbf{e}_{i'}^{(0)}, \forall i' \in \mathcal{N}(u) \right\} \right), \quad \mathbf{e}_i^{(1)} = \omega \left( \left\{ \mathbf{e}_{u'}^{(0)}, \forall u' \in \mathcal{N}(i) \right\} \right)$$

After two hops (Eq.2):

$$\mathbf{e}_u^{(2)} = \omega \left( \left\{ \mathbf{e}_{i'}^{(1)}, \forall i' \in \mathcal{N}(u) \right\} \right), \quad \mathbf{e}_i^{(2)} = \omega \left( \left\{ \mathbf{e}_{u'}^{(1)}, \forall u' \in \mathcal{N}(i) \right\} \right)$$

After three hops (Eq.3):

$$\mathbf{e}_u^{(3)} = \omega \left( \left\{ \mathbf{e}_{i'}^{(2)}, \forall i' \in \mathcal{N}(u) \right\} \right), \quad \mathbf{e}_i^{(3)} = \omega \left( \left\{ \mathbf{e}_{u'}^{(2)}, \forall u' \in \mathcal{N}(i) \right\} \right)$$







# Message-passing reformulation (2/2)

We rewrite Eq.2 and Eq.3 through Eq.1 and Eq.2:

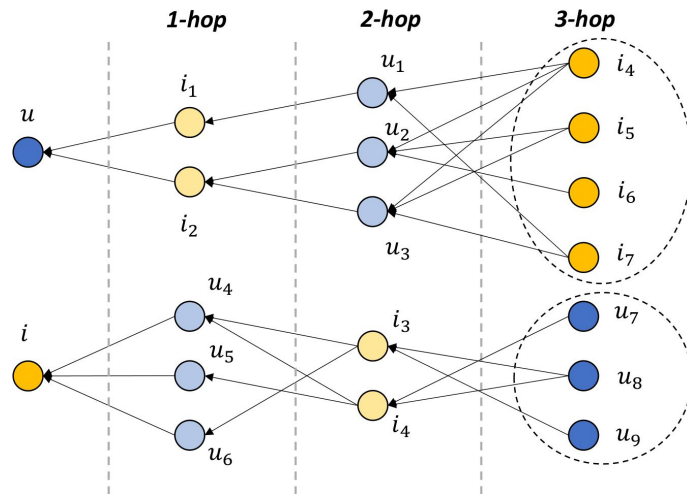
$$e_u^{(2)} = \omega \left( \left\{ \omega \left( \left\{ e_{u''}^{(0)}, \forall u'' \in \mathcal{N}(i') \setminus \{u\} \right\} \right), \forall i' \in \mathcal{N}(u) \right\} \right)$$

2-hop
1-hop

$$e_u^{(3)} = \omega \left( \left\{ \omega \left( \left\{ \omega \left( \left\{ e_{i'''}^{(0)}, \forall i''' \in \mathcal{N}(u'') \setminus \{i'\} \right\} \right), \forall u'' \in \mathcal{N}(i') \setminus \{u''\} \right\} \right), \forall i' \in \mathcal{N}(u) \right\} \right)$$

3-hop
2-hop
1-hop

**OBSERVATION:** Message-passing works on **same-** and **different-type** node explorations, where the **former** occur for **even** number of hops, the **latter** occur for **odd** number of hops.





# Experimental settings



# Datasets

Dataset	# Users	# Items	# Interactions	Sparsity
<i>Movielens-1M*</i>	5,915	2,753	570,622	0.9650
<i>Amazon Digital Music*</i>	8,328	6,275	99,400	0.9981
<i>Epinions*</i>	14,341	13,145	269,170	0.9986

\* Datasets have been pre-processed through score binarization (scores > 3 are considered as positive interactions) and filtered with the  $p$ -core strategy.



# Graph baselines

## Explicit message-passing

- Neural graph collaborative filtering (NGCF) [Wang et al., SIGIR 2019]
- Light graph convolutional network (LightGCN) [He et al., SIGIR 2020]
- Disentangled graph collaborative filtering (DGCF) [Wang et al., SIGIR 2020]
- Linear residual graph convolutional collaborative filtering (LR-GCCF) [Chen et al., AAI 2020]

## Implicit message-passing

- Ultra simplification of graph convolutional networks (UltraGCN) [Mao et al., CIKM 2021]
- Graph filter based collaborative filtering (GFCF) [Shen et al., CIKM 2021]



# Evaluation Metrics

## Accuracy

- $Recall@K$
- $nDCG@K$

## Novelty

- $EPC@K$  (expected number of recommended unknown items which are also relevant)
- $EFD@K$  (expected number of recommended known items which are also relevant)

## Diversity (how unequally a recommender shows different items to users)

- $Gini@K$
- $SE@K$



# Results and Discussion

(Amazon Digital Music)



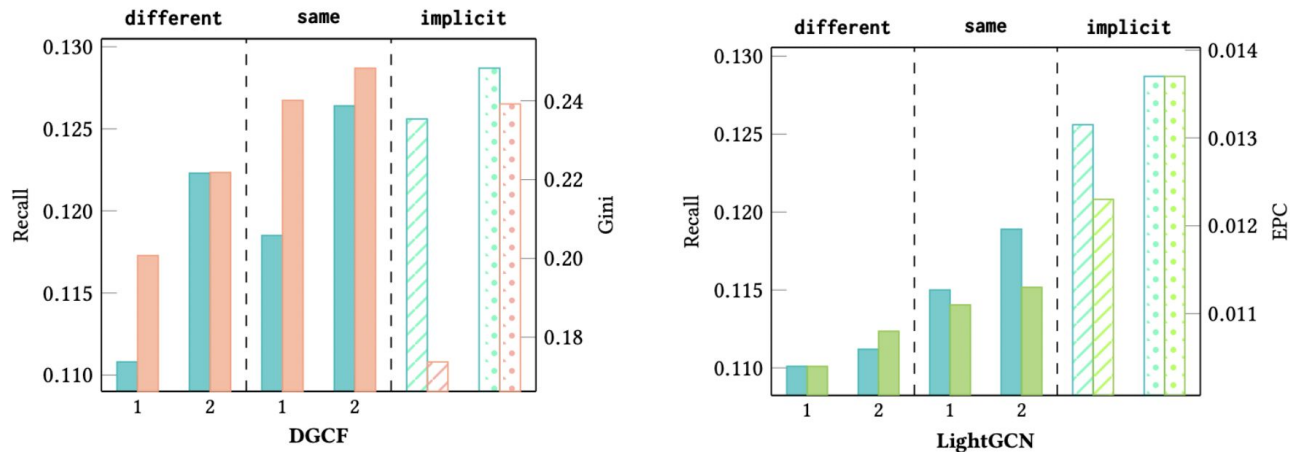
# RQ1: Overall recommendation performance

Models	Accuracy		Novelty		Diversity	
	<i>Recall</i>	<i>nDCG</i>	<i>EPC</i>	<i>EFD</i>	<i>Gini</i>	<i>SE</i>
<b>Explicit</b> message-passing						
NGCF	0.1127	0.0606	0.0109	0.1270	<b>0.4130</b>	<b>11.6953</b>
LightGCN	0.1189	0.0628	0.0113	0.1310	0.3148	11.2940
DGCF	<u>0.1264</u>	0.0674	<u>0.0123</u>	<u>0.1400</u>	0.2483	10.8904
LR-GCCF	0.1246	0.0664	0.0119	0.1388	<u>0.4037</u>	<u>11.6542</u>
<b>Implicit</b> message-passing						
UltraGCN	0.1256	<u>0.0675</u>	<u>0.0123</u>	0.1382	0.1737	10.0458
GFCF	<b>0.1287</b>	<b>0.0744</b>	<b>0.0137</b>	<b>0.1544</b>	0.2392	10.4923

**Observation 1:** While the **accuracy/novelty** trade-off does **not depend** on the explicit/implicit **message-passing**, the **accuracy/diversity** trade-off is preserved only when **explicitly propagating messages**, at the expense of (**limited**) recommendation **accuracy drops**.



## RQ2: A finer trade-off evaluation



**Observation 2:** To confirm observation 1, **explicit message propagation** (even at 1 hop) can reach a **better accuracy/diversity trade-off** than **implicit** propagation; then, **same-type** node explorations may lead to **improved accuracy/novelty and accuracy/diversity trade-offs**





# Conclusion and Future Work



## Conclusion

- Accuracy-novelty-diversity trade-off in graph collaborative filtering for different neighborhood exploration strategies and depths
- Accuracy-diversity trade-off better reached when explicitly propagating messages
- User-user and item-item interactions may be leveraged to reach the trade-off

## Future work

- Study other graph collaborative filtering approaches optimizing diversity
- Better investigate the same-type node exploration



# Thank you! How to reach us out...

Our official GitHub repository:



<http://github.com/sisinfab/Novelty-Diversity-Graph>



Contacts:

[vitowalter.anelli@poliba.it](mailto:vitowalter.anelli@poliba.it)

[yashar.deldioo@poliba.it](mailto:yashar.deldioo@poliba.it)

[tomaso.dinoia@poliba.it](mailto:tomaso.dinoia@poliba.it)

[eugenio.disciascio@poliba.it](mailto:eugenio.disciascio@poliba.it)

[antonio.ferrara@poliba.it](mailto:antonio.ferrara@poliba.it)

[daniele.malitesta@poliba.it](mailto:daniele.malitesta@poliba.it) (PRESENTER)

[claudio.pomo@poliba.it](mailto:claudio.pomo@poliba.it)